

# Emergent Behavior and Boid Swarms

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- ▶ Fractals
- ▶ Complex Systems and Chaos
- ▶ Emergent Behavior
- ▶ Natural Phenomenon
- ▶ Cellular Automata: Demonstration
- ▶ Boids & Flocking: Demonstration

# Fractals in Nature: *chou Romanesco*

Fractal forms are complex shapes which look more or less the same at a wide variety of scale factors, and are everywhere in nature.



# Fractal

a geometric figure consisting of an identical motif  
which repeats on an ever-reducing scale.

# Diving in to Veggies



# Look Closely — The Pattern Repeats!

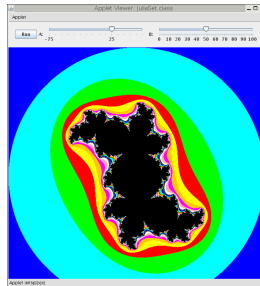
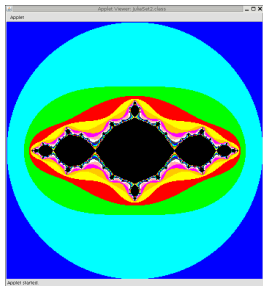
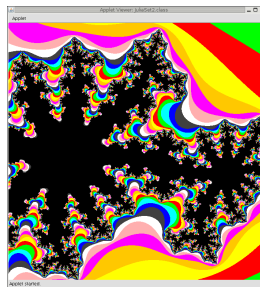
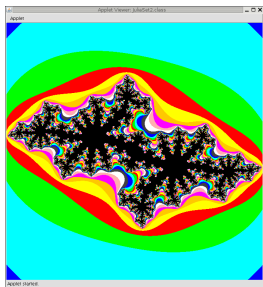


- ▶ A **fractal** may be a function that maps coordinates to values which we may then use to represent various colors, as in Julia Sets.
- ▶ **Julia Set** — To every real-valued pair,  $(a, b)$ , we can associate a function of two variables referred to as the Julia map for  $(a, b)$ , denoted by  $F_{a,b}$ , and described by the formula

$$F_{a,b}(x, y) = (x^2 - y^2 + a, 2xy + b).$$

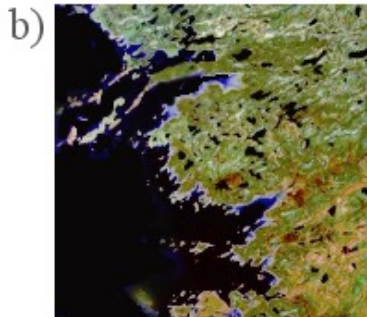
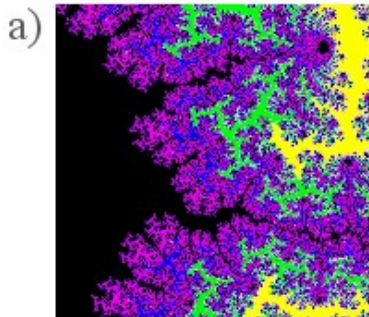
- ▶ The Julia set for  $(a, b)$ , denoted by  $J_{a,b}$ , is the collection of all points in the plane from which you can start and never get too far away from the origin by repeated iterations of  $F_{a,b}$ .

# Julia Set Examples — from CS I





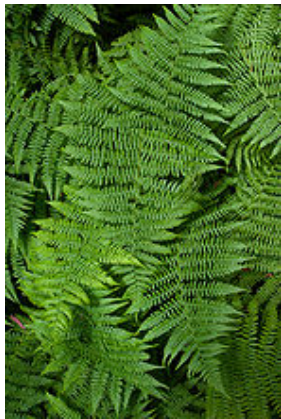
# Synthesizing Nature: Coastlines



a) Part of the Mandelbrot set.

b) Part of the North American coastline near Hudson Bay.

# Ferns



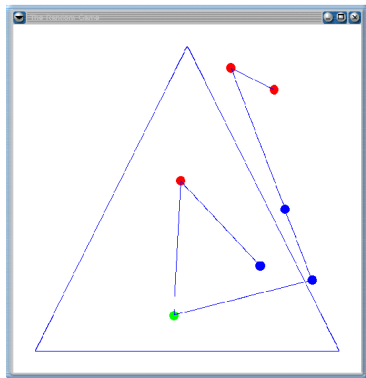
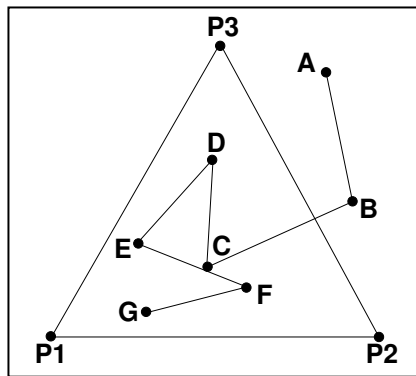
# Complex Systems and Chaos

- ▶ A **complex system** is composed of **interconnected parts** that **as a whole** exhibit one or more properties not obvious from the properties of the **individual parts**.
- ▶ One type of complex, dynamical system is a **chaotic** system: from chaos sometimes comes order!
- ▶ Simple Rule(s)  $\Rightarrow$  Complex Result.

# Sierpinski Gasket – also from CS I

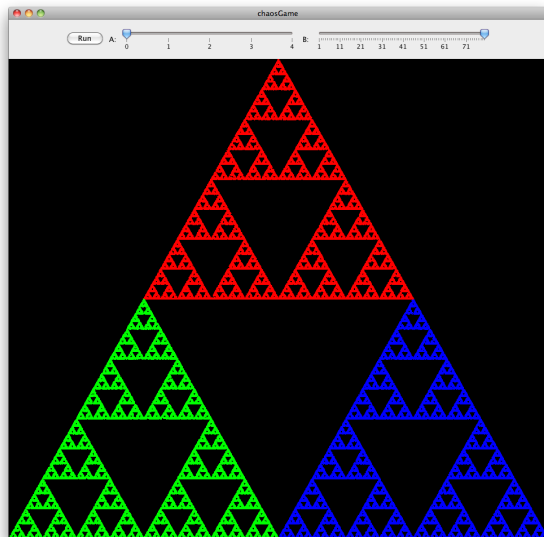
## The Chaos Game

Rule: Randomly pick a vertex and move halfway toward it.

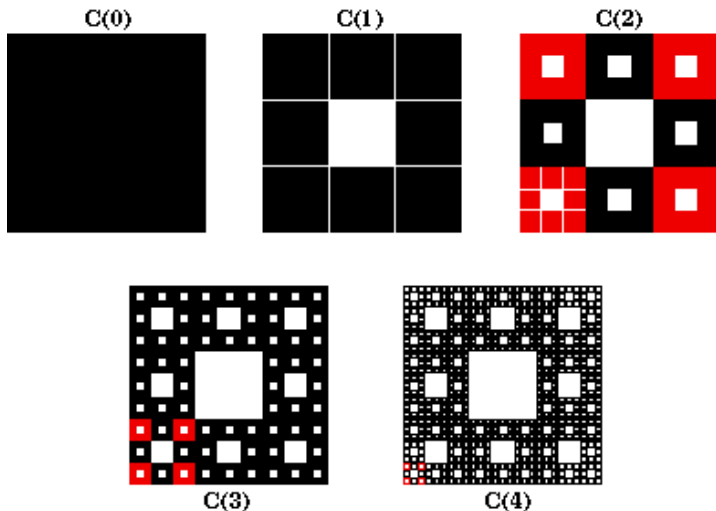


Color the new point according to which vertex was chosen.

# The Result:

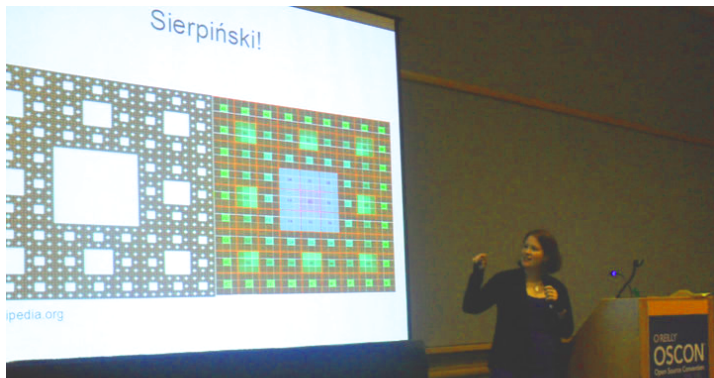


# Sierpinski Carpet

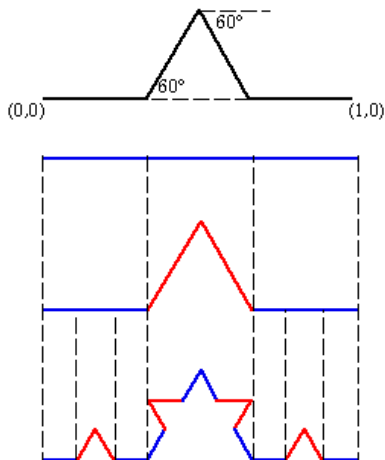


Rule: Subdivide square into  $3 \times 3$  squares, remove middle; Repeat.

# Sierpinski Carpet — and Quilt (OSCON, Australia)



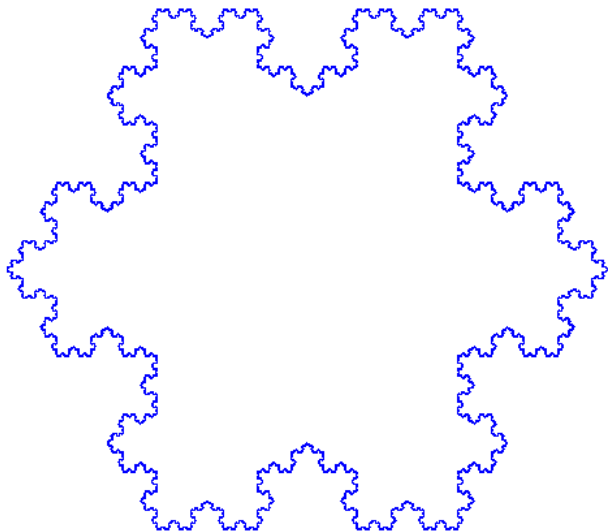
# The Koch Snowflake



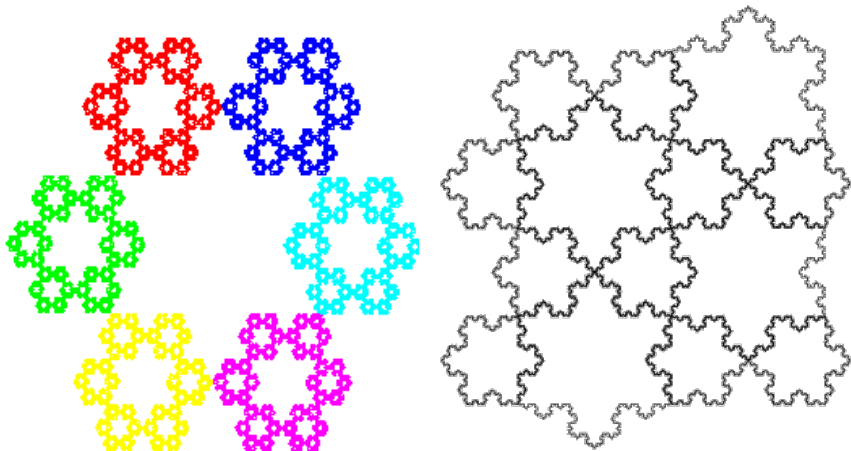
Rule: Replace the middle third of each line segment with 2 sides of an equilateral triangle.



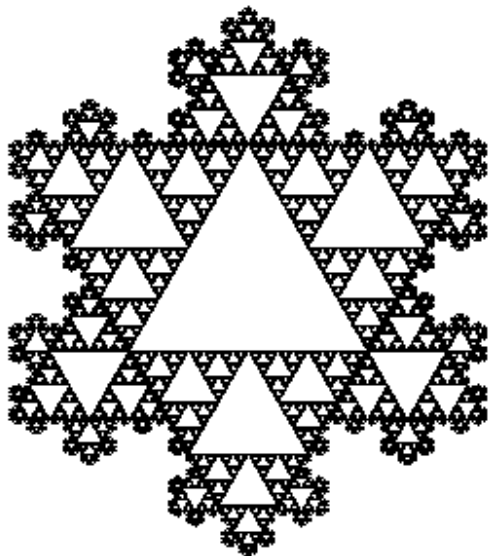
# The Koch Snowflake – Starting from a Triangle



# Tilings...



# Back to the Sierpinski Triangle!



# Emergent Behavior

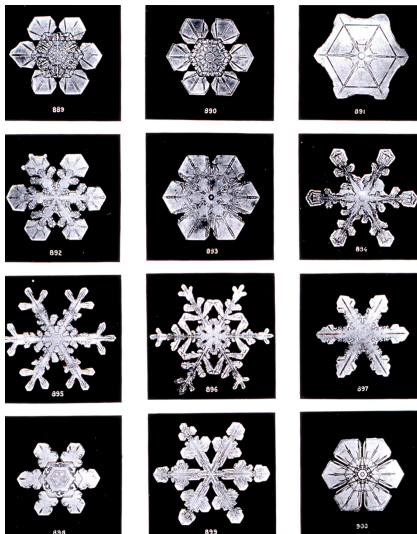
- ▶ A complex system is a network of heterogeneous components that interact non-linearly, to give rise to **emergent behavior**.
- ▶ The number of interactions between components of a system increases combinatorially with the number of components — (potentially) allowing for many new and subtle types of behavior to emerge.

- ▶ **Emergence** is the way complex systems and **patterns** arise out of a multiplicity of relatively simple interactions.
  
- ▶ An **emergent behavior** or **emergent property** can appear when a number of simple entities (agents) operate in an environment, forming more **complex behaviors** as a **collective**.

# Natural Phenomenon: Ice Crystals

**Water crystals** forming on glass  
is an emergent natural process — a  
**high level of organizational structure**  
crafted directly by the  
**random motion**  
of water molecules.

# Nature: Snowflakes



# Fractal: Frost





# Nature: Frost



# Chaos and Hexagons

The most interesting stable patterns appear  
right at the edge of chaos...

...a honeycomb arrangement of **hexagons**.

John Gribbin  
Deep Simplicity

# Hexagons Appear in Unexpected Places



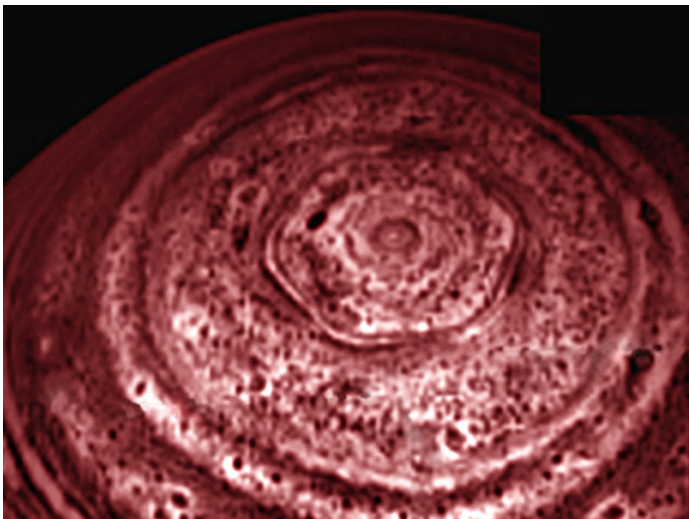
## Giant's Causeway, Ireland

About 40,000 interlocking basalt columns, the result of an ancient volcanic eruption.

# Fingal's Cave, Scotland



# Even in Space!



A hexagonal "feature" around Saturn's North Pole

# Creating a Hexagon in Fluid (Aliens Not Included)



Similar effect with buckets of water

A pentagonal "hole" in the center of water swirling against the edge of a rotating bucket.

A **hexagon** appears when the bucket is spun at a higher speed.

# Hexagons Are Everywhere!



# Hexagons Occur in Nature





# Some of Us Sport Our Own!



# Hexagons in the Home



Crochet Pattern

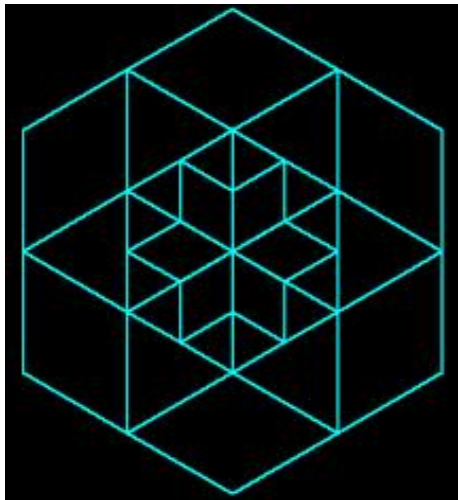


Crochet Colorfully Combined,  
Tiling the Plane

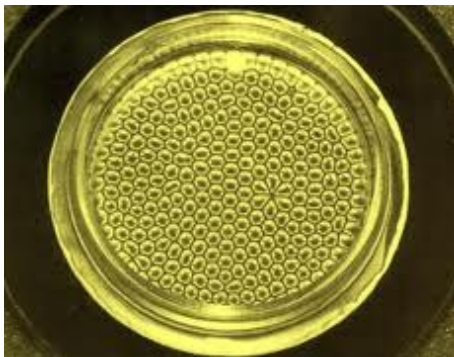
# Crochet: Sierpinski Pattern



# Quilt Block Patterns



# Hexagons in the Kitchen



## Bénard Convection

One can observe the formation of Bénard cells by heating a thin layer of oil in a pan.

# Termites

- ▶ Complex social systems may exhibit behaviors that are **emergent**.
- ▶ The mound building of termites is a property that emerges from the collection of termites.



# Termite Mounds



Classic examples of emergence in nature.

# And Then There Are the Ants...

First you see one...



Then a few more...



Then the deluge!





# 10 Tons of Concrete and 40 Tons of Dirt Later...

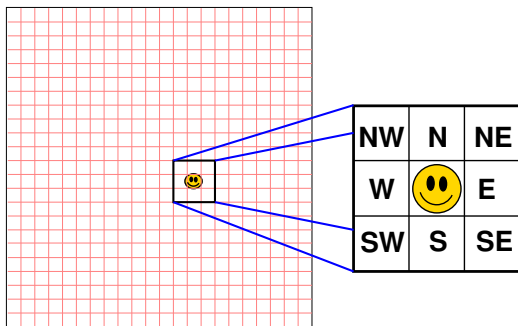


# Simulating Complex Systems: Cellular Automata

- ▶ A **cellular automaton** consists of a regular grid of **cells**, each in a finite number of **states**.
- ▶ The **neighborhood** of a cell is a set of cells defined relative to the specified cell.
- ▶ An **initial state** (time  $t = 0$ ) is created by assigning a state to each cell.
- ▶ A new **generation** is created (advancing  $t$  by 1), according to some fixed rule(s) that determines the new state of each cell in terms of the current states of the cell and its neighbors.

# Conway's Game of Life

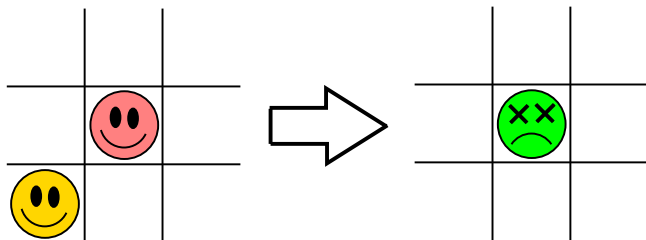
- ▶ A zero-player game (cellular automaton) devised by British mathematician John Horton Conway in 1970.
- ▶ Each cell on a grid has eight neighbors:



- ▶ There are four simple rules. . .

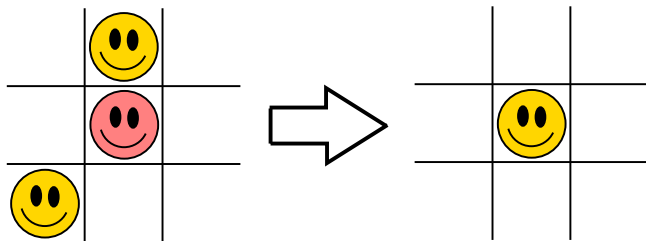
## Rule No. 1 — Loneliness

Any live cell with **fewer than two** live neighbors **dies**



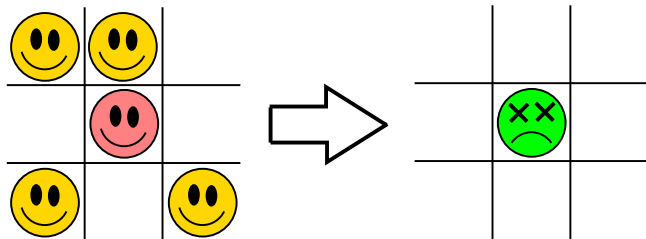
## Rule No. 2 — Balanced Life

Any live cell with **two or three** live neighbors **lives** on to the next generation



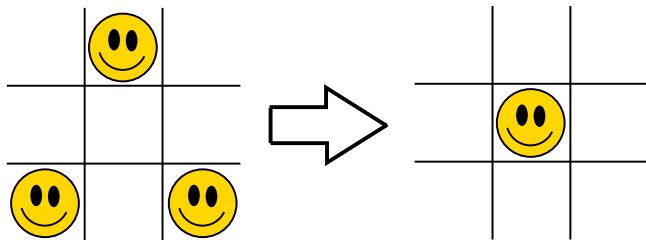
## Rule No. 3 — Overcrowding

Any live cell with **more than three**  
live neighbors **dies**



## Rule No. 4 — Reproduction

Any **dead** cell with **exactly three** live neighbors becomes a **live** cell



# The Game Of Life



# Complex Behavior

- ▶ As seen in the Game of Life, systems with **emergent properties or structures** may appear to defy entropic principles because they form and increase **order** despite the **lack** of **command** and **central control**.
- ▶ Open systems can extract information and order out of the environment.
- ▶ Another animation example is **boids**, which create swarming behavior in a simulated flock.

# Feeding Fail

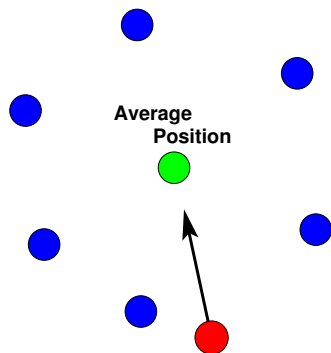


[http://chzgifs.files.wordpress.com/2011/03/  
fishmagnetsarerepulsedp1.gif](http://chzgifs.files.wordpress.com/2011/03/fishmagnetsarerepulsedp1.gif)

# Boids and Flocking

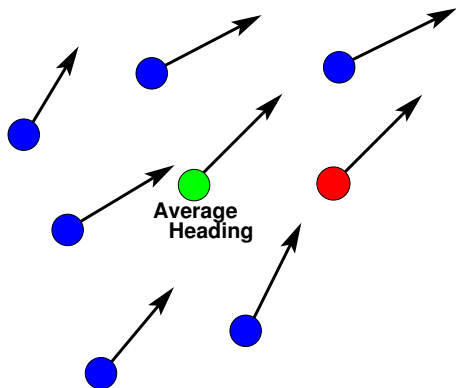
- ▶ There was a screen saver in UNIX some time ago, consisting of a **swarm** of short white lines which followed a red line around the screen much like a **school of fish** or **flock of birds**.
- ▶ In his 1987 SIGGRAPH paper "*Flocks, Herds, and Schools: A Distributed Behavioral Model*," Craig Reynolds coined the term **boids** to refer to this type of simulated flock.
- ▶ Boid flocks move in an extremely realistic way, creating complex motion and interaction.
- ▶ The behavior of boids is governed by simple rules. . .

## Boid Rule: Cohesion



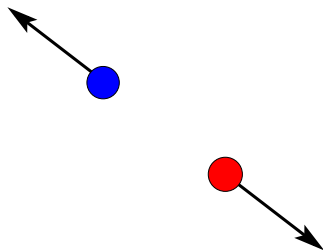
**Cohesion:** each unit steers toward the average position of its neighbors (stay with the group)

## Boid Rule: Alignment



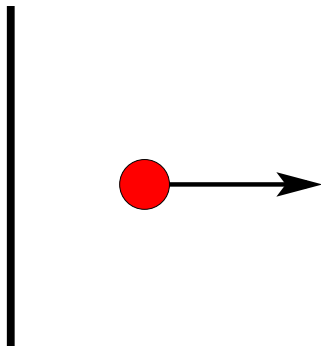
**Alignment:** each unit seeks to align itself to the average heading of its neighbors (move in the same direction)

## Boid Rule: Separation



**Separation:** each unit attempts to avoid hitting its neighbors  
(maintain some "personal" space)

## Boid Rule: Avoidance



**Obstacle Avoidance:** each unit attempts to avoid hitting obstacles (such as a wall or the mouse)

# Boid Program Controls

- ▶ The **separation**: how hard the boids try to maintain some "personal" space
- ▶ The **separation distance**: the ideal amount of personal space (in pixels).
- ▶ **Alignment**: how hard boids try to move in the same direction.
- ▶ **Cohesion**: how hard boids try to stay in a group.
- ▶ **Avoidance**: how hard the boids try to stay away from the walls and mouse.
- ▶ **Visible range**: how far each boid can "see."



# Flocking Program: Demonstration

<http://www.zemows.org/~mertz/flock/launch.jnlp>

# Control Settings with Interesting Results

<b>Simulates</b>	<b>Sep</b>	<b>Sep Dist</b>	<b>Align</b>	<b>Avoid</b>	<b>Cohesion</b>	<b>Vis</b>	<b>Boids</b>
bird flock	1	10	1	1	0.2	100	600
gnats	2	20	0.1	1	0.5	100	600
fish tank	3.0	20	1	3.0	0.5	100	12
gas	1	20	0.1	2	-0.1	100	900
min state	1	20	0	100	-50	100	400

## Other Examples

- ▶ <http://demonstrations.wolfram.com/ACellularAutomatonBasedHeatEquation/>
- ▶ <http://demonstrations.wolfram.com/GarbageCollectionByAnts/>
- ▶ <http://demonstrations.wolfram.com/FoodSearchingModelForAnts/>
- ▶ <http://demonstrations.wolfram.com/3DBoidModel/>
- ▶ <http://demonstrations.wolfram.com/ParticleSystemFountain/>
- ▶ <http://demonstrations.wolfram.com/topic.html?topic=Cellular+Automata&sortmethod=recent>

**Thank You!**

**Any Questions?**