Computer Problem 5.

- (a) Use the addition formulas for sin and cos to prove that $\tan(\pi/2 x) = 1/\tan x$.
- (b) Show that $[0, \pi/4]$ can be used as a fundamental domain for tan x.
- (c) Design a tangent key, following the principles of Program 3.3, using degree 3 polynomial interpolation on this fundamental domain.
- (d) Empirically estimate the maximum error of the tangent key in $[0, \pi/4]$.

Solution.