## Sec 3.3 Review

- \* A conditional statement uses implication ( $\rightarrow$ ) or if...else
- \*  $p \rightarrow q$  is false only when p is true and q is false.
- \*  $p \rightarrow q$  is equivalent to (~  $p \lor q$ )
- We can use Truth Tables to show two conditional expressions are equivalent (their truth values will be the same)
- \* A tautology is a statement which is always TRUE.
- Circuits in series correspond to conjunctions (ands)
- Circuits in parallel correspond to disjunctions (ors)
- \* Some circuits can be simplified.

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**Rewrite as Boolean Expressions and Simplify** 



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	Direct Statement	$p \to q$	If p, then q	
	Converse	$q \to p$	If q, then p	
	Inverse	$\sim$ p $\rightarrow$ $\sim$ q	If not p, then not	
	Contrapositive	$\sim$ q $\rightarrow \sim$ p	If not q, then not	
Dir Con	ect Statement ( $p  ightarrow q$ verse:	):		
Dire Con Inv	ect Statement ( $p \rightarrow q$ verse: erse:	):		



Rolling stones gather no moss.

Birds of a feather flock together.

2. r implies s

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3. If r, then s

1. r only if s

4. r is necessary for s

others... Which one is it?

A triangle is equilateral only if it has three equal sides.

One of the following statements is not equivalent to the

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## **Consistent or Contrary?**

Two statements about the same object are: consistent — if they are both true. contrary — if they cannot both be true.

- 1. The car is a Chevy. The car is a Toyota.
- 2. Elvis is alive. Elvis is dead.
- 3. The animal has four legs. The animal is a dog.
- 4. The cake is chocolate. The cake has two layers.
- 5. The clock is broken. The clock has the right time.
- 6. The math class meets at noon. The math class lasts 50 minutes.
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- 7. The number is an integer. The number is irrational.
- 8. The punch is pink. The punch has juice in it.
- 9. President Bush is a Republican. President Bush is a Democrat.
- 10. The sofa is soft. The sofa is blue.
- 11. The plant is blooming. The plant is dead.
- 12. The dog ate my homework. The dog bites.
- 13. That rock is igneous. That rock is sedimentary.
- 14. That bird is a robin. That bird is blue.

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## **Biconditionals** Biconditional: compound statement of the form p if and only if q, written $p \leftrightarrow q$ or p iff q. $\mathsf{p} \leftrightarrow \mathsf{q} \text{ is equivalent to } (\mathsf{p} \rightarrow \mathsf{q}) \land (\mathsf{q} \rightarrow \mathsf{p})$ $\begin{array}{c} \mathsf{or} \\ \mathsf{p} \leftrightarrow \mathsf{q} \equiv (\mathsf{p} \rightarrow \mathsf{q}) \wedge (\mathsf{q} \rightarrow \mathsf{p}) \end{array}$ Truth Table for $p \leftrightarrow q$ $q \mid p \leftrightarrow q$ р Т Т Т ΤF F F Т F F F Т © 2005-09, N. Van Cleave 15

In Summary						
$\sim$ p	<b>negation</b> of p	truth value is opposite of p				
p∧q	conjunction	true only when both p and q are true				
$p \lor q$	disjunction	false only when both p and q are false				
$p \to q$	conditional	false only when p is true and q is false				
p ↔ q	biconditional	true only when p and q have the <b>same</b> truth value				

True or False?								
A biconditional is both statements o	true are fai	only when bo Lse.	oth stat	ements are	true or			
True or False:	5 = 9 -	- 4 if and only	if 8+2	= 10				
True or False:	Clintor	n was presiden	t IFF Ca	rter wasn't	president.			
True or False:	IBM s	ells computer:	s iff Piz	za Hut sells	Big Macs.			
True or False:	8+7	15 IFF 3×5	9.					

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