

## Stack: An Abstract Data Type

An important abstraction that you will encounter in many applications.

We will describe three uses:
Interrupt-Driven I/O

- The rest of the story...

Evaluating arithmetic expressions

- Store intermediate results on stack instead of in registers

Data type conversion

- 2' s comp binary to ASCII strings


## Stacks

A LIFO (last-in first-out) storage structure.

- The first thing you put in is the last thing you take out.
- The last thing you put in is the first thing you take out.

This means of access is what defines a stack, not the specific implementation.

Two main operations:
PUSH: add an item to the stack
POP: remove an item from the stack

## A Physical Stack

## Coin rest in the arm of an automobile



Initial State


After
One Push


After Three
More Pushes


After
One Pop

First quarter out is the last quarter in.

## A Hardware Implementation

## Data items move between registers

| Empty: Yes | Empty: No |  | Empty: No |  | Empty: No |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1/1/11 | $\leftarrow$ TOP | \#18 | $\leftarrow$ TOP | \#12 | $\leftarrow$ TOP | \#31 | $\leftarrow$ TOP |
| 1/1111 |  | 1/1/1/ |  | \#5 |  | \#18 |  |
| 1/1111 |  | 1/1111 |  | \#31 |  | 1/1/11 |  |
| 1/1/11 |  | 1/1/11 |  | \#18 |  | 1/1111 |  |
| 1/1111 |  | 1/1111 |  | /1/1/1 |  | 1/1111 |  |
| Initial State |  | After One Push |  | After Thre More Pushes |  | After Two Pops |  |

## A Software Implementation

Data items don't move in memory, just our idea about there the TOP of the stack is.

| 1/1/11 | $\leftarrow$ TOP | 1/1/11 | $\leftarrow$ TOP | \#12 | $\leftarrow$ TOP | \#12 | $\leftarrow$ TOP |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1/1111 |  | 1/1111 |  | \#5 |  | \#5 |  |
| 1/1111 |  | 1/1111 |  | \#31 |  | \#31 |  |
| 1/1111 |  | \#18 |  | \#18 |  | \#18 |  |
| 1/1/11 |  | 1/1/1/ |  | /////1 |  | /////1 |  |
| x4000 | R6 | x3FFF | R6 | x3FFC | R6 | x3FFE | R6 |
| Initial State |  | After One Push |  | After Three More Pushes |  | After Two Pops |  |

By convention, R6 holds the Top of Stack (TOS) pointer.

## Basic Push and Pop Code

For our implementation, stack grows downward (when item added, TOS moves closer to 0 )

Push
ADD R6, R6, \#-1 ; decrement stack ptr STR RO, R6, \#O ; store data (RO)

Pop
LDR R0, R6, \#0 ; load data from TOS
ADD R6, R6, \#1 ; decrement stack ptr

## Pop with Underflow Detection

If we try to pop too many items off the stack, an underflow condition occurs.

- Check for underflow by checking TOS before removing data.
- Return status code in R5 (0 for success, 1 for underflow)

```
POP LD R1, EMPTY ; EMPTY = -x4000
    ADD R2, R6, R1 ; Compare stack pointer
    BRz FAIL ; with x3FFF
    LDR R0, R6, #0
    ADD R6, R6, #1
    AND R5, R5, #0 ; SUCCESS: R5 = 0
    RET
FAIL AND R5, R5, #0 ; FAIL: R5 = 1
    ADD R5, R5, #1
    RET
EMPTY .FILL xCOOO
```


## Push with Overflow Detection

If we try to push too many items onto the stack, an overflow condition occurs.

- Check for underflow by checking TOS before adding data.
- Return status code in R5 (0 for success, 1 for overflow)

```
PUSH LD R1, MAX ; MAX = -x3FFB
    ADD R2, R6, R1 ; Compare stack pointer
    BRz FAIL ; with x3FFF
    ADD R6, R6, #-1
    STR R0, R6, #0
    AND R5, R5, #0 ; SUCCESS: R5 = 0
    RET
FAIL AND R5, R5, #0 ; FAIL: R5 = 1
    ADD R5, R5, #1
    RET
MAX .FILL xCOO5
```


## Interrupt-Driven I/O (Part 2)

Interrupts were introduced in Chapter 8.

1. External device signals need to be serviced.
2. Processor saves state and starts service routine.
3. When finished, processor restores state and resumes program.

## Interrupt is an unscripted subroutine call, triggered by an external event.

Chapter 8 didn' t explain how (2) and (3) occur, because it involves a stack.

Now, we' re ready...

## Processor State

What state is needed to completely capture the state of a running process?
Processor Status Register

- Privilege [15], Priority Level [10:8], Condition Codes [2:0]

| 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{P}$ |  |  |  |  |  | PL |  |  |  |  |  |  | $\mathbf{N}$ | $\mathbf{Z}$ | P |

## Program Counter

- Pointer to next instruction to be executed.


## Registers

- All temporary state of the process that's not stored in memory.


## Where to Save Processor State?

Can' t use registers.

- Programmer doesn't know when interrupt might occur, so she can' t prepare by saving critical registers.
- When resuming, need to restore state exactly as it was.

Memory allocated by service routine?

- Must save state before invoking routine, so we wouldn't know where.
- Also, interrupts may be nested that is, an interrupt service routine might also get interrupted!

Use a stack!

- Location of stack "hard-wired".
- Push state to save, pop to restore.


## Supervisor Stack

A special region of memory used as the stack for interrupt service routines.

- Initial Supervisor Stack Pointer (SSP) stored in Saved.SSP.
- Another register for storing User Stack Pointer (USP): Saved.USP.

Want to use R6 as stack pointer.

- So that our PUSH/POP routines still work.

When switching from User mode to Supervisor mode (as result of interrupt), save R6 to Saved.USP.

## Invoking the Service Routine - The Details

1. If Priv = 1 (user),

Saved.USP = R6, then R6 = Saved.SSP.
2. Push PSR and PC to Supervisor Stack.
3. Set PSR[15] = 0 (supervisor mode).
4. Set PSR[10:8] = priority of interrupt being serviced.
5. Set PSR[2:0] = 0 .
6. Set MAR $=x 01 \mathrm{vv}$, where $\mathrm{vv}=8$-bit interrupt vector provided by interrupting device (e.g., keyboard = x80).
7. Load memory location (M[x01vv]) into MDR.
8. Set PC = MDR; now first instruction of ISR will be fetched.

Note: This all happens between the STORE RESULT of the last user instruction and the FETCH of the first ISR instruction.

## Returning from Interrupt

Special instruction - RTI - that restores state.

RTI | 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

1. Pop $P C$ from supervisor stack. $(P C=M[R 6] ; R 6=R 6+1)$
2. Pop PSR from supervisor stack. (PSR = M[R6]; $R 6=R 6+1$ )
3. If $\operatorname{PSR}[15]=1, R 6=$ Saved.USP.
(If going back to user mode, need to restore User Stack Pointer.)

RTI is a privileged instruction.

- Can only be executed in Supervisor Mode.
- If executed in User Mode, causes an exception. (More about that later.)


## Example (1)



Executing ADD at location x3006 when Device B interrupts.

## Example (2)



Saved.USP = R6. R6 = Saved.SSP. Push PSR and PC onto stack, then transfer to Device B service routine (at x6200).

## Example (3)



Executing AND at x6202 when Device C interrupts.

## Example (4)

| R6 $\rightarrow$x6203 <br> PSR for B <br> x3007 <br> PSR for A <br> $/ / 1 / / 1$ |
| :--- |
| PC $\mathbf{x 6 3 0 0}$ |



Push PSR and PC onto stack, then transfer to Device C service routine (at x6300).

## Example (5)



Execute RTI at x6315; pop PC and PSR from stack.

## Example (6)



Execute RTI at x6210; pop PSR and PC from stack. Restore R6. Continue Program A as if nothing happened.

## Exception: Internal Interrupt <br> When something unexpected happens <br> inside the processor, it may cause an exception.

## Examples:

- Privileged operation (e.g., RTI in user mode)
- Executing an illegal opcode
- Divide by zero
- Accessing an illegal address (e.g., protected system memory)

Handled just like an interrupt

- Vector is determined internally by type of exception
- Priority is the same as running program


## Arithmetic Using a Stack

Instead of registers, some ISA's use a stack for source and destination operations: a zero-address machine.

- Example:

ADD instruction pops two numbers from the stack, adds them, and pushes the result to the stack.

Evaluating $(A+B) \cdot(C+D)$ using a stack:
(1) push $A$
(2) push B
(3) ADD
(4) push C
(5) push D
(6) ADD
(7) MULTIPLY
(8) pop result

```
Why use a stack?
- Limited registers.
- Convenient calling convention for subroutines.
- Algorithm naturally expressed using FIFO data structure.
```


## Example: OpAdd POP two values, ADD, then PUSH result.



## Example: OpAdd

| OpAdd | JSR POP | $;$ Get first operand. |
| :--- | :--- | :--- |
|  | ADD R5,R5,\#0 | $;$ Check for POP success. |
|  | BRp Exit | $;$ If error, bail. |
|  | ADD R1,R0,\#0 | $;$ Make room for second. |
|  | JSR POP | ; Get second operand. |
|  | ADD R5,R5,\#0 | $;$ Check for POP success. |
|  | BRp Restore1 | $;$ If err, restore \& bail. |
|  | ADD R0,R0,R1 | $;$ Compute sum. |
|  | JSR RangeCheck | ; Check size. |
|  | BRp Restore2 | $;$ If err, restore \& bail. |
|  | JSR PUSH | $;$ Push sum onto stack. |
|  | Restore2 | ADD R6,R6,\#-1 |
| Restore1 | ADD R6,R6,\#-1 | Decr stack ptr (undo POP) |
| Exit | RET |  |

## Data Type Conversion

Keyboard input routines read ASCII characters, not binary values.
Similarly, output routines write ASCII.
Consider this program:

| TRAP | x23 | ; input from keybd |
| :--- | :--- | :--- |
| ADD | R1, R0, \#0 | ; move to R1 |
| TRAP | x23 | ; input from keybd |
| ADD | R0, R1, R0 | ; add two inputs |
| TRAP | x21 | ; display result |
| TRAP | x25 | ; HALT |

User inputs 2 and 3 -- what happens?
Result displayed: e
Why? ASCII '2' (x32) + ASCII '3' (x33) = ASCII 'e' (x65)

## ASCII to Binary

Useful to deal with mult-digit decimal numbers Assume we've read three ASCII digits (e.g., "259") into a memory buffer.

How do we convert this to a number we can use?

| x32 | '2' |
| :---: | :---: |
| $\mathbf{x 3 5}$ | '5' |
| x39 | ' $9 '$ |

- Convert first character to digit (subtract x30) and multiply by 100.
- Convert second character to digit and multiply by 10.
- Convert third character to digit.
- Add the three digits together.


## Multiplication via a Lookup Table

How can we multiply a number by 100 ?

- One approach: Add number to itself 100 times.
- Another approach:

Add 100 to itself <number> times. (Better if number < 100.)

Since we have a small range of numbers (0-9),
use number as an index into a lookup table.
Entry 0: $0 \times 100=0$
Entry 1: $1 \times 100=100$
Entry 2: $2 \times 100=200$
Entry 3: $3 \times 100=300$ etc.

## Code for Lookup Table

; multiply RO by 100, using lookup table ;

LEA R1, Lookup100 ; R1 = table base
ADD R1, R1, R0 ; add index (R0)
LDR R0, R1, \#0 ; load from M[R1]

Lookup100 .FILL 0 ; entry 0
.FILL 100 ; entry 1
.FILL 200 ; entry 2
.FILL 300 ; entry 3
.FILL 400 ; entry 4
.FILL 500 ; entry 5
.FILL 600 ; entry 6
.FILL 700 ; entry 7
.FILL 800 ; entry 8
.FILL 900 ; entry 9

## Complete Conversion Routine (1 of 3)

; Three-digit buffer at ASCIIBUF.
; R1 tells how many digits to convert.
; Put resulting decimal number in RO.
ASCIItoBinary AND R0, RO, \#0 ; clear result ADD R1, R1, \#0 ; test \# digits
BRz DoneAtoB ; done if no digits

LD R3, NegZero ; R3 = -x30
LEA R2, ASCIIBUF
ADD R2, R2, R1
ADD R2, R2, \#-1 ; points to ones digit

LDR R4, R2, \#0 ; load digit ADD R4, R4, R3 ; convert to number ADD R0, R0, R4 ; add ones contrib

## Conversion Routine (2 of 3)

| ADD $1, R 1, \#-1$ | ; one less digit |
| :--- | :--- |
| BRz DoneAtoB | ; done if zero |
| ADD $R 2, R 2, \#-1$ | $;$ points to tens digit |

LDR R4, R2, \#0 ; load digit
ADD R4, R4, R3 ; convert to number
LEA R5, Lookup10 ; multiply by 10
ADD R5, R5, R4
LDR R4, R5, \#0
ADD R0, R0, R4 ; adds tens contrib

ADD R1, R1, \#-1 ; one less digit
BRz DoneAtoB ; done if zero
ADD R2, R2, \#-1 ; points to hundreds
; digit

## Conversion Routine (3 of 3)

| LDR | R4, R2, \#0 ; load digit |
| :--- | :--- | :--- |
| ADD | R4, R4, R3 ; convert to number |
| LEA | R5, Lookup100 ; multiply by 100 |
| ADD | R5, R5, R4 |
| LDR | R4, R5, \#0 |
| ADD | R0, R0, R4 ; adds 100 's contrib |

;
DoneAtoB
NegZero
ASCIIBUF
Lookup10

Lookup100
.FILL 0
.FILL 100

## Binary to ASCII Conversion

Converting a 2's complement binary value to a three-digit decimal number

- Resulting characters can be output using OUT

Instead of multiplying, we need to divide by 100 to get hundreds digit.

- Why wouldn't we use a lookup table for this problem?
- Subtract 100 repeatedly from number to divide.

First, check whether number is negative.

- Write sign character (+ or -) to buffer and make positive.


## Binary to ASCII Conversion Code (part 1 of 3)

; RO is between -999 and +999.
; Put sign character in ASCIIBUF, followed by three
; ASCII digit characters.

| BinaryToASCII | LEA R1, ASCIIBUF ; pt to result string |
| :--- | :--- |
|  | ADD R0, R0, \#0 |
|  | BRn NegSign |
|  | LD R2, ASCIIplus ; store 't' |
|  | STR R2, R1, \#0 |
| NegSign | BRnzp Begin100 |
|  | LD R2, ASCIIneg ; store '-' |
|  | STR R2, R1, \#0 |
|  | NOT R0, R0 |
|  | ADD R0, R0, \#1 |

## Conversion (2 of 3)

| Begin100 | LD R2, ASCIIoffset |
| :--- | :--- |
| Loop100 | LD R3, Neg100 |
|  | ADD R0, R0, R3 |
|  | BRn End100 |
| End100 | ADD R2, R2, \#1 ; add one to digit |
|  | BRnzp Loop100 |
|  | STR R2, R1, \#1 ; store ASCII 100's digit |
|  | LD R3, Pos100 |
|  | ADD R0, R0, R3 ; restore last subtract |
|  |  |
|  | LD R2, ASCIIoffset |
|  | LD R3, Neg10 |
|  | ADD R0, R0, R3 |
|  | BRn End10 |
|  | ADD R2, R2, \#1 ; add one to digit |
|  | BRnzp Loop10 |

## Conversion Code (3 of 3)

| End10 | $\begin{array}{lll} \text { STR R2, } & R \\ \text { ADD R0, } \end{array}$ | R1, \#2 ; store ASCII 10's digit <br> R0, \#10 ; restore last subtract |
| :---: | :---: | :---: |
| ; |  |  |
|  | LD R2, A | ASCIIoffset |
|  | ADD R2, R2 | R2, R0 ; convert one's digit |
|  | STR R2, R1 | R1, \#3 ; store one's digit |
|  | RET |  |
| ; |  |  |
| ASCIIplus | .FILI x2B | ; plus sign |
| ASCIIneg | .FILL x2D | ; neg sign |
| ASCIIoffset | .FILL x30 | ; zero |
| Neg100 | .FILL xFF9C | ; -100 |
| Pos100 | .FILL \#100 |  |
| Neg10 | .FILL xFFF6 | ; -10 |

